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OXY-HEMOGLOBIN DISSOCIATION CURVES OF WHOLE BLOOD IN ANEMIA

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Although the oxy-hemoglobin dissociation curves of normal whole blood have been extensively studied for many years (1, 2, 3), there has been relatively little investigation of these curves in the blood of abnormal subjects.

Meakins, Dautrebande and Fetter (4), in their work on circulatory stasis in 1923, published some oxygen dissociation curves of patients with cardiac decompensation, showing that at or near 40 mm. CO₂ tension, these curves did not deviate appreciably from those of normal blood. Stadie and Martin (5), investigating carbon monoxide hemoglobin and oxy-hemoglobin relations, included one oxygen dissociation curve of a patient with pernicious anemia. This was at 40 mm. CO₂ tension, and was an apparently normal curve. Odaira (6) stated that in severe anemia the oxygen curves were lowered, but did not state at what CO₂ tension or serum pH these curves were determined.

The present investigation represents a study of the oxy-hemoglobin dissociation curves of the whole blood of several subjects with anemia from various causes, and of one with advanced polycythemia vera. It comprises the following: (a) at serum pH (or pH_s) 7.44 (CO₂ tension approximately 40 mm.), points on the O₂ dissociation curves of five primary anemias, two secondary anemias, and one polycythemia vera; (b) at pH_s 7.64 (CO₂ tension approximately 20 mm.), points on the curves of three primary and two secondary anemias; (c) at pH_s 7.24 (CO₂ tension approximately 80 mm.), points on the curves of one primary and one secondary anemia. A control curve of the blood of one of us was also done at each of these CO₂ tensions.

METHODS

Blood was drawn from an arm vein, with stasis of one minute or less, into a container with enough neutralized dried potassium oxalate, and dried sodium fluoride to make a concentration of approximately 0.2 per cent of the former and 0.1 per cent of the latter. Tonometers of 300 cc. capacity were filled with the desired CO₂ and O₂ mixtures by the manometer method outlined by Van Slyke, Wu and McLean (7). Five cubic centimeters of blood were introduced into each tonometer. Two tonometers were then put into a water bath at 38, \pm 0.2°C., and rotated for forty minutes or more. The other tonometers were put in the ice box, and equilibrated later. The gases in the equilibrating tonometers were brought to atmospheric pressure at 38°, by allowing excess gas to escape at the beginning of the equilibration and again after about ten minutes of rotating. The effect of equilibrating the blood in the tonometers for longer than forty minutes was tested on the blood of one of us (see table 1, experiment of March 29th) at an oxygen tension of 20 mm. There was no measurable change in the oxygen capacity of the blood in the tonometers after either two hours' or four hours' rotation. After equilibration the blood was withdrawn directly into 1 cc. stopcock-pipettes, and then transferred for oxygen or CO₂ determination to a Van Slyke-Neill constant volume apparatus. Samples of the tonometer gases were collected in gas sampling tubes and their CO₂ and O₂ contents determined later by the Haldane gas analysis apparatus. The above procedure is in general that of the "first saturation method" of Austin, Cullen *et al.* (8).

In two of the earlier experiments, the blood was collected from the tonometers into test tubes under oil. Under these conditions, however, the blood was found to absorb oxygen and lose CO₂, especially if stirring was necessary, as was usually the case on account of the rapid settling of anemic blood. The transfer of blood directly to pipettes saved one step in manipulation; was easily accomplished by connecting three or four pipettes successively to the tonometer by a bent glass tube connection, and drawing the blood into them; and this method gave duplicate determinations that checked satisfactorily. A pipette full of blood could be left standing several minutes without measurably changing the O₂ content.

Oxygen capacity determinations were in most cases made after equilibrating the blood in air at room temperature; occasionally in tonometers at 38°C.; the proper value for dissolved O₂ being applied in each case.

There was considerably greater difficulty in obtaining an accurate curve from a markedly anemic blood than from normal blood. This was partly because of the rapidity of settling of the red cells, and partly because of the magnification of errors in per cent oxygen saturation when the oxygen capacity was small. In the first two of our primary anemia curves at 40 mm. CO₂ tension, in which the blood after equilibration was collected under oil, our duplicate determinations did not check closely. In the succeeding experiments, a total of 61 points on abnormal blood curves were determined: duplicate determinations on two of them checked only to 0.4 volume per cent; four others to 0.3 volumes per cent; and

four points were based on a single oxygen content determination. Duplicate measurements for the other points checked within the error of the method, 0.2 volumes per cent. Of 31 points on our control blood, three checked only to 0.4 volumes per cent, the rest within the error of the method. An exception is made of the case of W. B., (table 3), a secondary anemia whose major condition was myelogenous leukemia. His white blood count was 700,000; and his blood was found to diminish rapidly in O_2 content on standing; so that we were compelled to use for our curve only the first oxygen measurement after equilibration of the blood, the first pipetteful of blood being transferred as rapidly as possible from the tonometer to a Van Slyke apparatus containing air-free ferricyanide solution.

CORRECTIONS

The form of the dissociation curve of oxy-hemoglobin has been shown, by Adair (9) and others, to depend primarily on the pH of the solution, although the content of bicarbonate and other electrolytes also influences the levels of the curves to some extent (10, 11, 1). For the comparison of oxygen dissociation curves of the whole blood of different individuals, it would therefore probably be best to have all curves corrected to the same cell pH (or pH_c). Such corrections can be made, as fairly good approximations, by the use of the Donnan ratio r , as developed by Van Slyke, Wu and McLean (7), if the pH_c and percentage oxygen saturation are known. When these corrections are worked out, however, using the data of Bock, Field and Adair (3), it is found that the differences between the curves at constant pH_c , at constant pH_s , and at constant CO_2 tension, are small; and although the larger corrections are outside the limits of the experimental error, they are smaller than the recognized and as yet unexplained differences between the blood of different normal individuals. We have, therefore, in these curves simply determined the pH_s of the oxygenated blood at the desired CO_2 tension, 20, 40, or 80 mm., and if this pH_s value has differed by more than 0.04 from that of the standard normal curves, a correction has been applied to all the points on that curve. Four of the curves, one primary anemia, two secondary anemias, and one control blood, required such a correction. The corrections have been made in the O_2 tension by interpolation, using the curves of Bock, Field, and Adair as standards.

The pH_s was determined gasometrically, by the Henderson-Hasselbalch formula. The CO_2 content of the oxygenated blood at the

desired CO₂ tension was determined by measuring the CO₂ content (either whole blood or "true" serum) of the blood in the tonometer having the highest O₂ tension. This blood was, in the various cases, from 90 to 98 per cent saturated with oxygen. The CO₂ tension, as measured, varied usually a few millimeters from the exact value desired, i.e., 20, 40, or 80. A small extrapolation on the CO₂ curve, with correction for oxygen unsaturation, then gave the CO₂ content of fully oxygenated blood at the exact CO₂ tension, with sufficient accuracy. In some of the determinations we measured the whole blood CO₂ content and in others that of the "true" serum. In the former case the pH_s was determined by the method outlined by Van Slyke, Wu and McLean (7), using their Δ pK' values. We used 6.13 as the pK' value, and $\alpha_{\text{CO}_2} = 0.555$ per Kg of blood water for the solubility factor, as employed by Van Slyke, Hastings, Murray and Sendroy (12). These constants gave slightly different pH_s values to our curves, and also to the curves of Bock, Field, and Adair, than when computed by using the constants of Van Slyke's earlier paper (7).

In as much as in our gas equilibrations we used the "first saturation method" of Austin, Cullen, *et al.* (8), the CO₂ tensions in the tonometers were only approximately correct and the Haldane analyses after equilibration frequently showed the final CO₂ tensions to be several millimeters from the desired tensions of 20, 40, or 80 mm. A correction formula was developed on the basis of the empirical linear relation between CO₂ tension and 1/K of Hill's equation, a relation which L. J. Henderson (13) found to be approximately true when applied to Barcroft's blood curves, and which he expressed in the formula: $\frac{p_{\text{CO}_2} + 7.7}{0.014} = \frac{\text{Hb}}{\text{HbO}_2} (p_{\text{O}_2})^{2.5}$. The correction formula which we have used is the same in principle as that used by Bock, Field and Adair, and is, for the 40 mm. curves, as follows:

$$\log p_{\text{O}_2,40} = \frac{1}{2.5} \log [(40 + 7.7) + 2.5 \log p_{\text{O}_2} - \log (p_{\text{CO}_2} + 7.7)]$$

where $p_{\text{O}_2,40}$ = O₂ tension at 40 mm. CO₂ tension

p_{O_2} = O₂ tension as measured

p_{CO_2} = CO₂ tension as measured.

As a matter of fact, except in the cases of the larger corrections, especially those near 100 per cent oxygen saturation, little difference was found between the corrections, based on the above formula, and those found merely by interpolation, using as standards the curves of Bock, Field and Adair. The method of interpolation, being simpler, was therefore usually employed for the smaller corrections.

DISCUSSION

The data for all the curves are tabulated in tables 1, 2 and 3, and the points charted in figures 1 to 3. The drawn curves in the figures, included for purposes of comparison, are reproduced from the data of Bock, Field and Adair, the continuous lines being from the blood of A. V. B. and the interrupted line from that of G. S. A. Clinical data in regard to the patients studied are given in table 4.

It will be seen that all the $pH_s = 7.44$ curves fall fairly close to the normal ones, both for primary and secondary anemias. There is perhaps a tendency for the anemic curves to lie at a little lower level, especially in the upper part of their course, than the normals. The polycythemia curve shows no evidence of abnormality.

The points on the $pH_s = 7.24$ curves also are fairly close to each other; the normal curve here, however, does not agree as well with that of A. V. B. We have no special comment to offer on this latter point, except that for some reason a smooth and accurate curve is, in general, more difficult to obtain at this high CO_2 tension. Bock, Field, and Adair encountered the same thing in their work. In our final normal control experiment, all oxygen determinations were done in triplicate, and the average of the closest two values were taken for each point.

At the more alkaline reaction of $pH_s = 7.64$ there are obviously distinct differences between the curves of the individuals studied. The number of curves is, of course, small, and it is therefore quite possible that the variations in the levels of the curves simply represent variations that might occur between the oxygen dissociation curves of any small group of normal individuals. That such differences do occur has been known since Barcroft's early work (1). It is clear from an examination of figure 2, however, that our normal control curve is close to that of A. V. B., and that the anemia curves

TABLE 1

Subject	Condition	Date	CO ₂ tension mm.	O ₂ tension mm.	Total O ₂ vols. per cent	HbO ₂ per cent	P _{O₂} (at P _{CO₂} = 40 mm.) mm.	P _{O₂} (at pH _s = 7.44) mm.	
D. W. R. Male 30	Normal subject	April 30	46.0	136.0	21.5	100.0	—	Total CO ₂ , oxygenated blood (at P _{CO₂} = 40 mm.) = 49.1 vols. per cent, pH _s = 7.46 Cell volume = 45 per cent Oxygen capacity = 0.47 Cell vol. per cent	
			air	air	22.3	100.0	—		
			39.7	15.3	4.7	21.6	15.3		
		March 1	36.1	22.7	9.7	44.0	23.7		—
			37.6	62.8	20.6	93.5	65.0		—
			38.0	73.7	21.2	96.3	75.9		—
		March 16	35.9	33.4	14.6	66.5	34.4		—
			39.8	42.1	17.2	78.3	42.1		—
			42.2	52.7	19.5	89.0	52.2		—
		March 29	42.9	87.8	21.4	97.3	86.5		—
			44.3	4.0	1.5	6.9	4.0		—
			41.3	7.6	1.8	8.2	7.6		—
		March 29	air	air	22.3	100.0	—		—
			air	air	22.8	100.0	—		—
			44.0	25.6	10.2	45.2	24.9		—
March 29	air	air	22.9	100.0	—	—			
	43.6	24.1	10.0	44.1	23.5	—			
	air	air	22.8	100.0	—	—			
air	air	43.6	24.3	10.0	44.4	23.5			

M. C. Male, 62	Pernicious anemia	March 9	44.4	38.7	7.9	68.5	37.7	34.1	Total CO ₂ , oxygenated blood (true serum) (at P _{CO₂} = 40 mm.) = 49.0 vols. per cent, pH _s = 7.36	
			44.4	6.7	0.9	7.9	7.8	6.6		
			44.0	58.2	10.2	88.5	57.2	52.8		
			44.2	18.6	2.9	25.9	18.0	15.8		
			44.6	75.8	10.8	93.0	74.5	70.1		
			59.4	70.9	—	—	—	—		
			air	air	11.9	100.0	—	—		
			air	air	16.9	100.0	—	—		
			40.6	11.9	2.8	17.1	11.9	—		
			39.6	29.3	9.2	55.5	29.3	—		
23.2	39.0	13.9	84.0	48.0	—					
H. Sa. Male 39	Pernicious anemia	February 26	air	air	8.8	100.0	—	—	Total CO ₂ , oxygenated blood (at P _{CO₂} = 40 mm.) = 53.5 vols per cent, pH _s = 7.43 Cell volume = 14 per cent Oxygen capacity = 0.59 Cell vol. per cent	
			38.1	59.7	7.7	90.4	61.0	—		
			37.1	24.2	3.6	42.8	24.7	—		
			air	air	8.7	100.0	—	—		
			40.7	60.2	7.7	91.4	60.0	—		
			40.5	51.3	7.1	85.3	51.2	—		
			38.6	31.4	4.9	58.5	31.8	—		
			39.9	23.8	3.2	38.5	23.8	—		
			air	air	14.1	100.0	—	—		
			36.6	72.1	13.2	95.5	75.7	—		
C. G. Female 67	Pernicious anemia	March 26	37.6	42.8	10.5	76.3	43.8	—	pH _s = 7.44 (March 26), 7.46 (April 2), 7.46 (April 9) Cell volume (March 26) 14.5 per cent Oxygen capacity = 0.57 Cell vol. per cent	
			air	air	13.5	100.0	—	—		
			42.4	11.5	2.7	20.6	11.2	—		
			32.1	82.3	12.7	96.2	89.2	—		
			42.4	21.8	5.1	38.8	21.4	—		
		April 2	April 9	air	air	14.1	100.0	—		—
				36.6	72.1	13.2	95.5	75.7		—
				37.6	42.8	10.5	76.3	43.8		—
				air	air	13.5	100.0	—		—
				42.4	11.5	2.7	20.6	11.2		—

TABLE 1—Continued

Subject	Condition	Date	CO ₂ tension mm.	O ₂ tension mm.	Total O ₂ vols. per cent	HbO ₂ per cent	P _{O₂} (at P _{CO₂} = 40 mm.) mm.	P _{O₂} (at p _{H₂} = 7.44) mm.	Total CO ₂ , oxygenated blood (at P _{CO₂} = 40 mm.) = 46.6 vols. per cent, p _{H₂} = 7.48 Cell volume = 62 per cent Oxygen capacity = 0.43 Cell vol. per cent = 0.43
M. J. Female 52	Polycythemia vera	April 16	air	air	27.4	100.0	—	—	Total CO ₂ , oxygenated blood (at P _{CO₂} = 40 mm.) = 60.0 vols. per cent, p _{H₂} = 7.48 Cell volume not done
			43.0	71.6	25.3	93.2	70.8		
			32.7	26.0	14.2	52.4	27.8		
			39.6	13.8	5.1	19.0	13.8		
			40.4	47.0	22.5	83.2	47.0		
V. S. Female 41	Secondary anemia	April 23	air	air	8.5	100.0	—	—	Total CO ₂ , oxygenated blood (at P _{CO₂} = 40 mm.) = 7.48 per cent, p _{H₂} = 7.48 Cell volume not done
			38.6	52.5	7.2	88.7	53.6		
			46.3	65.3	7.5	91.3	61.7		
			43.3	10.1	1.3	16.2	9.8		
			April 22						
			38.7	30.2	4.7	57.5	30.6		
			41.7	69.3	7.9	96.2	68.5		
A. O. Female 38	Pernicious anemia	March 17	24.9	150.0	4.6	100.0	—	—	p _{H₂} = 7.46 (March 17), 7.43 (March 26) Cell volume (March 17) = 5.5 vols. per cent
			36.8	24.2	2.3	51.6	25.0		
			37.4	45.5	3.6	83.3	46.8		
			32.5	71.6	4.2	95.0	76.3		

TABLE 2

Subject	Condition	Date	CO ₂ tension mm.	O ₂ tension mm.	Total O ₂ vols. per cent	HbO ₂ per cent	P _{O₂} (at P _{CO₂} = 20 mm.) mm.	P _{O₂} (at pH _s = 7.64) mm.
D. W. R. Male 30	Normal subject	April 30	22.0	15.9	6.7	31.6	15.5	pH _s (April 30) = 7.67. pH _s ("diluted blood") (at P _{CO₂} = 27.5) = 7.59 Cell volume (April 30) = 45 per cent O ₂ capacity = 0.47 Cell vol. per cent Cell volume ("diluted blood") = 28 per cent Oxygen capacity = 0.48 Cell vol. per cent
			22.8	37.7	17.3	81.2	36.3	
			25.2	65.2	20.7	96.3	59.5	
			46.0	136.0	21.5	100.0	—	
			23.4	46.3	19.0	89.0	43.2	
		May 22	20.3	11.8	3.9	18.1	11.8	
			22.2	23.5	11.9	55.4	22.9	
			air	air	21.8	100.0	—	
			26.3	35.5	10.8	79.1	36.0	
			28.6	72.7	13.5	98.0	71.7	
"Diluted blood"	June 3	27.7	20.7	6.2	45.4	20.7		
		27.9	9.3	2.1	15.6	19.4		
		air	air	14.1	100.0	9.0		
		air	air	12.4	100.0	—		
		23.5	28.7	7.4	61.3	27.6		
H. Sm. Female 78	Pernicious anemia	May 17	23.9	67.8	11.4	95.0	63.7	Total CO ₂ , oxygenated blood (true serum) (at P _{CO₂} = 20 mm.) = 42.5 vols. per cent, pH _s = 7.60 Cell volume = 23 per cent Oxygen capacity = 0.52 Cell vol. per cent
			29.1	11.6	1.9	16.0	10.7	
			23.6	49.3	10.6	87.9	47.0	
			21.7	19.0	4.7	39.5	18.7	
			23.6	49.3	10.6	87.9	47.0	

A. O. Female 38	Pernicious anemia	May 25	air	air	air	8.8	100.0	—	Total CO ₂ , oxygenated blood (at Pco ₂ = 20 mm.) = 45.5 vols. per cent, pH _a = 7.68
			23.0	21.1	20.5	3.4	38.0	20.5	
			23.7	51.8	49.4	8.0	88.5	49.4	
			22.6	35.8	34.8	6.8	76.0	34.8	
H. St. Female 49	Pernicious anemia	May 27	air	air	air	9.9	100.0	—	Total CO ₂ , oxygenated blood (at Pco ₂ = 20 mm.) = 39.0 vols. per cent, pH _a = 7.61 Cell volume = 19 per cent Oxygen capacity = 0.50 Cell vol. per cent
			17.6	76.9	78.5	9.2	95.7	78.5	
			21.1	11.4	11.4	1.3	13.9	11.4	
			23.8	20.2	19.0	3.2	33.7	19.0	
			16.0	36.6	38.8	7.7	80.5	38.8	
24.0	61.7	57.5	8.9	92.5	57.5				
M. S. Male 29	Bacterial endo- carditis, second- ary anemia	June 9	air	air	—	8.7	100.0	—	Total CO ₂ , oxygenated blood (at Pco ₂ = 20 mm.) = 48.5 vols. per cent, pH _a = 7.70
			20.0	20.2	20.0	3.7	44.3	20.0	
			25.2	33.2	30.7	6.2	73.8	30.7	
			20.1	10.6	10.6	1.5	18.2	10.6	
			18.9	71.9	79.0	8.1	96.4	73.0	
V. G. Female 31	Secondary anemia	June 30	air	air	—	10.2	100.0	—	Total CO ₂ , oxygenated blood (at Pco ₂ = 20 mm.) = 40.8 vols. per cent, pH _a = 7.65 Cell volume = 22.5 per cent Oxygen capacity = 0.43 Cell vol. per cent
			21.5	22.1	21.7	4.4	44.3	21.7	
			24.1	36.5	34.9	7.3	74.2	34.9	
			22.3	67.5	—	Lost	—	—	
			—	—	—	—	—	—	

TABLE 3

Subject	Condition	Date	CO ₂ tension mm.	O ₂ tension mm.	Total O ₂ vols. per cent	HbO ₂ per cent	Po ₂ (at pCO ₂ = 80 mm.) mm.
D. W. R. Male 30	Normal subject	June 23	air	air	21.4	100.0	—
			80.1	32.3	9.5	45.0	32.3
			79.3	51.1	15.7	74.0	51.3
			78.1	17.1	3.3	15.0	17.3
			79.0	76.4	18.8	89.0	76.7
A. O. Female 39	Pernicious anemia	June 19	air	air	20.6	100.0	—
			116.9	21.6	3.8	18.7	18.9
			79.9	41.9	12.6	62.1	41.9
			81.1	61.4	16.8	83.0	61.1
			80.2	85.3	18.8	92.5	85.3
W. B. Male 38	Myelogenous leukemia, secondary anemia	May 5	air	air	10.2	100.0	—
			47.2	63.5	8.0	80.4	61.7
			41.7	7.5	0.4	4.1	7.5
			42.9	40.1	5.4	54.6	39.5
			43.5	22.6	2.3	22.7	22.3

Total CO₂, oxygenated blood (true serum) (at pCO₂ = 80 mm.) = 77.3 vols. per cent, pH_s = 7.24
Cell volume = 42 per cent
Oxygen capacity = 0.48
Cell vol. per cent

Total CO₂, oxygenated blood (at pCO₂ = 80 mm.) = 63.5 vols. per cent, pH_s = 7.24

Total CO₂, oxygenated blood (at Pco₂ = 80 mm.) = 63.6 vols. per cent, pH_s = 7.21

Cell volume = 27 per cent
Oxygen capacity = 0.46
Cell vol. per cent

Total CO₂, oxygenated blood (at Pco₂ = 40 mm.) = 36.0 vols. per cent pH_s = 7.21
Cell volume = 55 per cent (large fraction was white blood cells)

are all at a definitely lower level. As far as these data are concerned, therefore, the probability is high that the condition of anemia is associated in some way with a lowering of the oxygen dissociation curve, when the pH_s is in the region of 7.64.

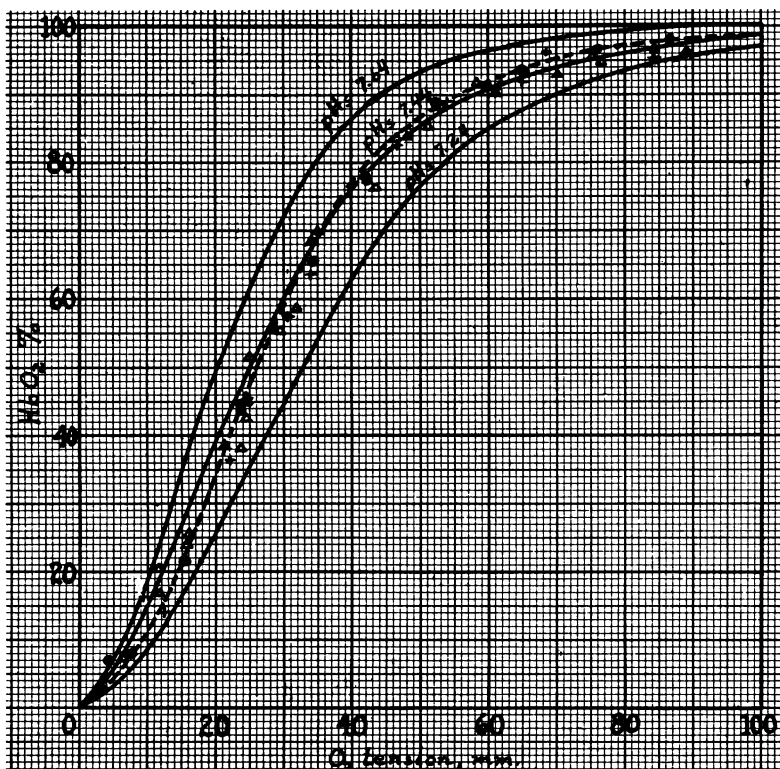


FIG. 1. OXY-HEMOGLOBIN DISSOCIATION CURVES AT pH_s 7.44 (CO_2 TENSION APPROXIMATELY 40 MM.)

Drawn curves from data of Bock, Field, and Adair. Heavy dots, normal control. Triangles (Δ), pernicious anemias. Plus marks (+), secondary anemias.

This can be more clearly shown if the points are plotted logarithmically (on the principle of Hill's equation), with coördinates $\log \frac{Hb}{HbO_2}$ and $\log p_{O_2}$. This has been done in figure 4, with a curve

TABLE 4

Subject	Sex	Age	Condition	Date	Blood counts		Transfusions	
					Red blood cells	Hemoglobin	Date	Amount
M. C.	M.	62	Pernicious anemia	February 12	600,000	18	February 12	800
				15	900,000	26		
				27	1,300,000	35		
A. O.	F.	38	Pernicious anemia	April 16	700,000	14	April 17	800
				27	1,500,000	20		
				May 21	1,400,000	27		
				June 1 5	2,600,000 3,200,000	30 42		
C. G.	F.	67	Pernicious anemia	March 25	1,300,000	40	March 27	500
				April 5	1,600,000	60		
H. St.	F.	49	Pernicious anemia	March 22	1,700,000	30	March 8	800
				May 24	2,900,000	45		
				June 1	3,100,000	42		
H. Sa.	M.	39	Pernicious anemia	February 13	2,200,000	63		
H. Sm.	F.	78	Pernicious anemia, chronic cholecystitis	April 28	1,500,000	35	May 6 15	540 700
				May 18	2,500,000	50		
V. S.	F.	41	Hematemesis, secondary anemia	April 21 28	2,300,000 2,800,000	40 35	April 29	500
P. L.	M.	38	Chronic nephritis, secondary anemia	May 6	3,800,000	70		

W. B.	M.	38	Myelogenous leukemia, secondary anemia	May 7	3,800,000*	60
M. J.	F.	52	Polycythemia vera	April 17	9,000,000	120
V. G.	F.	31	Menorrhagia, secondary anemia	June 18 23 26 July 1	2,500,000 1,800,000 3,000,000 3,500,000	20 40 35 45
M. S.	M.	30	Bacterial endocarditis, secondary anemia	June 6 22	2,400,000 2,300,000	30 40

* W. B. C. 700,000; myelocytes 51 per cent.

drawn through the points of normal blood, and another through those of the anemic bloods. The anemia curve is throughout its course lower than the normal.

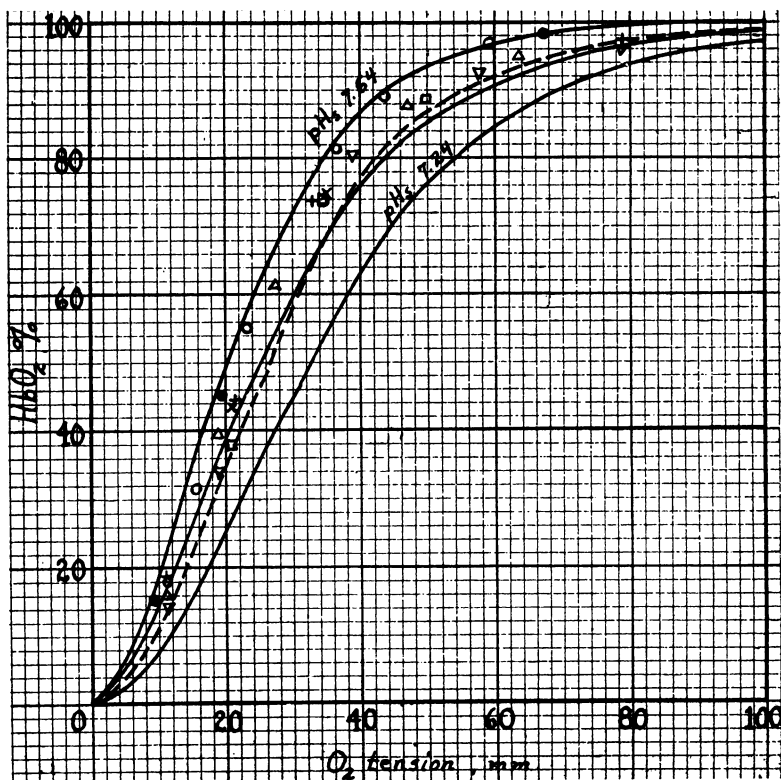


FIG. 2. OXY-HEMOGLOBIN DISSOCIATION CURVES AT pH_s 7.64 (CO_2 TENSION APPROXIMATELY 20 MM.)

Drawn curves from data of Bock, Field, and Adair. Circles, normal control. Heavy dots, normal control blood "diluted." Squares and triangles, pernicious anemias. Crosses and plus marks, secondary anemias.

To summarize, the data which we have obtained indicate that at pH_s of 7.24 and 7.44 there are no large consistent differences between the oxy-hemoglobin dissociation curves of normal and of anemic whole bloods; but that at pH_s of 7.64, the anemic curves are at a lower (more "acid") level than those of normal blood.

One would not expect simple dilution of the blood with serum to be responsible for a lowering of the curves; and this was easily shown to have practically no such effect. A sample of normal

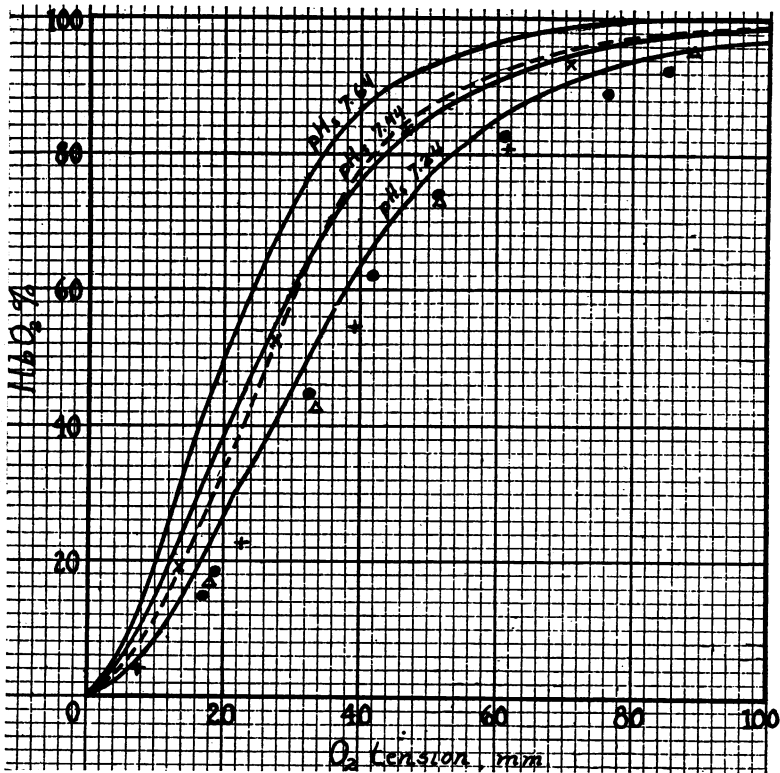


FIG. 3. OXY-HEMOGLOBIN DISSOCIATION CURVES AT pH_s 7.24 (CO₂ TENSION APPROXIMATELY 80 MM.)

Drawn curves from data of Bock, Field, and Adair. Heavy dots, normal control. Triangles, primary anemia. Plus marks, secondary anemia. Crosses are points on the curve of a patient with polycythemia vera, at CO₂ tension of 40 mm.

oxalated blood was centrifuged, a part of the cells mixed with the whole of the serum, and a dissociation curve determined for this diluted blood. The points, given in table 2, "diluted blood," and charted in figure 2, fell along the normal whole blood curve.

If instead one were to assume a concentration of the hemoglobin within the blood cell, a change, of the type found in our alkaline

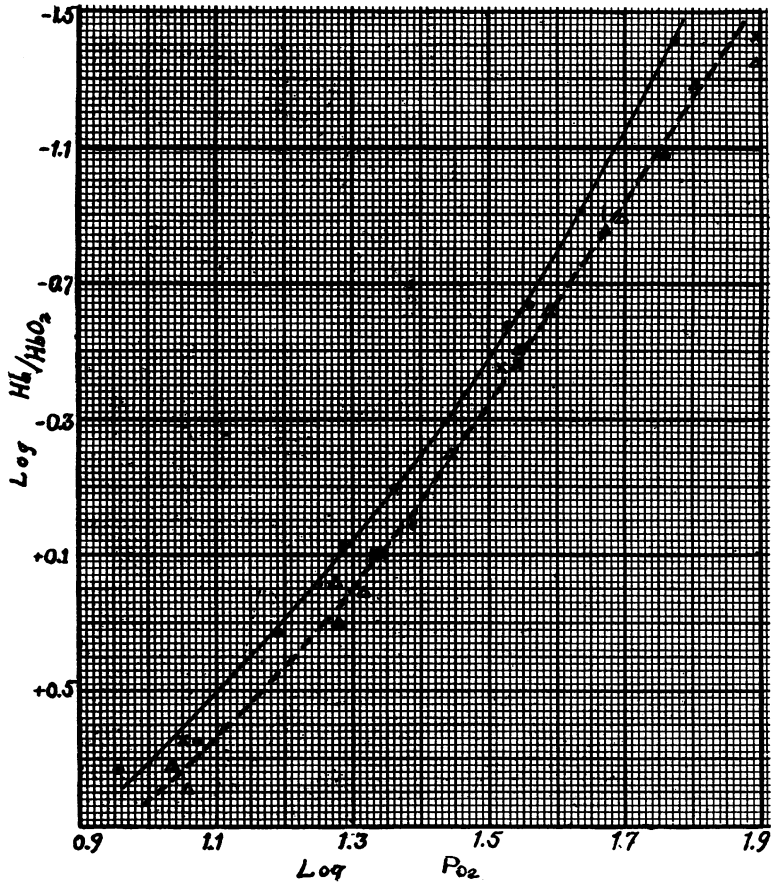


FIG. 4. OXY-HEMOGLOBIN DISSOCIATION CURVES OF WHOLE BLOOD AT pH_s 7.64, PLOTTED LOGARITHMICALLY

Heavy dots and continuous curve, normal control blood. Triangles, pernicious anemias. Crosses, secondary anemias. Dotted line, average curve for anemic blood.

anemia curves, would occur, and the displacement would be greater, the more alkaline the pH_s . This would be true because an increase in the hemoglobin concentration within the cell would increase the

Donnan effect; that is, the Van Slyke r would diminish and the difference between the cell pH and serum pH ($\text{pH}_s - \text{pH}_c$, or $-\log r$) would increase. Thus at equal pH_s values, the pH_c of the blood with increased cell hemoglobin would be lower than the pH_c of normal blood. The oxygen dissociation curve would therefore be at a lower level. Furthermore, the relative lowering would be greater the more alkaline the pH_s , the $\frac{-\log r}{\text{pH}_s}$ ratio having a steeper slope for blood with increased cell hemoglobin than for normal blood. This latter follows indirectly from the large increase in the dissociation of the cell protein (i.e. $[\text{BP}]_c$), when the solution becomes more alkaline. We have worked out these effects quantitatively using the Van Slyke, Wu, and McLean formula: $r = 1 - \frac{[\text{BP}]_c + [\text{HB}]_c - [\text{BP}]_s}{2([\text{B}]_s - [\text{BP}]_s)}$, and the data from the four experiments of the same paper; assuming, for the blood with increased cell hemoglobin, values of $[\text{BP}]_c$ and $[\text{Hb}]_c$ 4/3 times the given normal values. These computations give consistent results in all the four experiments; an average set of values is the following from experiment 3 (oxygenated blood):

pH_s	$-\log r (= \text{pH}_s - \text{pH}_c)$	
	Blood with increased cell hemoglobin	Normal blood
7.75	0.32	0.24
7.42	0.21	0.16
7.08	0.12	0.10

Thus, whereas at a pH_s of 7.08, the pH_c of the blood with increased cell hemoglobin is only 0.02 more acid than that of normal blood, at a pH_s of 7.75 there is a difference of 0.08. The differences are probably actually larger than those tabulated, because the pH_c figures of normal blood were determined in these experiments by Van Slyke, Wu and McLean from the $\frac{[\text{HCO}_3]_c}{[\text{HCO}_3]_s}$ ratios, and these ratios were considerably lower in most cases than the r values as determined by the formula for r given above. As we have said, we used this formula to determine the pH_c values of the blood with increased cell hemo-

globin. That the true $\frac{[\text{H}^+]_s}{[\text{H}^+]_o}$ ratio (or, more accurately, the ratio of the activity coefficients) is not equal to $\frac{[\text{HCO}_3]_c}{[\text{HCO}_3]_s}$, but is considerably less, has been shown recently by Van Slyke, Hastings, Murray, and Sendroy (12).

The above calculations are of course only rough approximations: the formula for r is itself only approximate, and the suggested changes in values of $[\text{BP}]_o$ and $[\text{Hb}]_o$ take no account of corresponding changes in other intracellular electrolyte concentrations, which would modify to some extent the percentage oxygen saturation of the hemoglobin. The figures given, however, do indicate the direction of the change that might be expected to occur, if concentration of hemoglobin within the cell were one of the conditions prevailing in a given blood. The figures also show the considerable increase in this effect when the blood becomes more alkaline.

If the concentration of hemoglobin within the cell did occur in anemia, one would expect it particularly in the primary types, with high $\frac{\text{oxygen capacity}}{\text{hematocrit}}$ ratios. Our data on this point are not very satisfactory. Hematocrit readings were obtained with the blood of two of the primary anemias at pH_s 7.64, giving $\frac{\text{oxygen capacity}}{\text{hematocrit}}$ ratios of 0.52 and 0.50, as compared with 0.47 for our normal control. This difference is in the expected direction, but not large enough to account for all the lowering of these two oxygen dissociation curves. We obtained a hematocrit reading from one of the secondary anemias at pH_s 7.64, giving an $\frac{\text{oxygen capacity}}{\text{hematocrit}}$ value of 0.43. This does not agree with the concentration hypothesis: the dissociation curve of this subject was lower than the normal, and yet the concentration of hemoglobin in the cell, according to the hematocrit, is less than normal. All our hematocrit values, however, are at best only approximate, as in our hands this instrument was not reliable. For this reason, it is hardly justifiable to use these values for purposes of calculation.

Determination of the electrolyte distribution in the blood of the

subjects studied was outside the scope of this investigation: reference to the data of Peters, Bulger, Eisenman and Lee (14), showed no indication of any large, consistent variation in the electrolytes of the blood of primary or secondary anemia that might account for low oxygen dissociation curves. Gram (15) has shown that the cell chloride concentration in anemia does not vary in any regular manner with the extent of the anemia.

We wish especially to express our gratitude to Professor L. J. Henderson and Dr. C. D. Murray, in collaboration with whom this work was planned, and with whom we had the privilege of discussing our results; and to Dr. A. B. Hastings, for guidance through many technical difficulties.

SUMMARY

The oxy-hemoglobin dissociation curves of the whole blood of several subjects with anemia, primary and secondary, were investigated at serum pH's of 7.24, 7.44 and 7.64. At the lower pH values, all curves studied were close to curves of normal blood. At serum pH 7.64 the anemia curves were definitely lower than the normal. One possible explanation of this fact is discussed.

Points on the curve of a patient with polycythemia vera showed no evidence of abnormality.

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